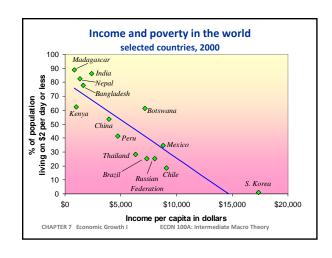
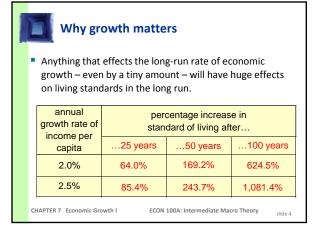


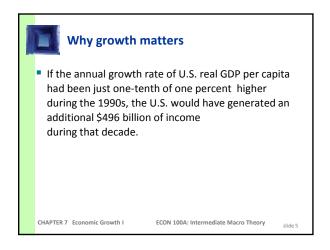
Why growth matters

Data on infant mortality rates:
20% in the poorest 1/5 of all countries
0.4% in the richest 1/5
In Pakistan, 85% of people live on less than \$2/day.
One-fourth of the poorest countries have had famines during the past 3 decades.
Poverty is associated with oppression of women and minorities.

Economic growth raises living standards and reduces poverty....
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### The lessons of growth theory

...can make a positive difference in the lives of hundreds of millions of people.



These lessons help us

- understand why poor countries are poor
- design policies that can help them grow
- learn how our own growth rate is affected by shocks and our government's policies

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### **Levels vs. Growth Rates**

- In this lecture, we will see several common transformations of key macroeconomic variables.
- Consider the following measures, in levels

	Description	Symbol	Data Equivalent
	(Aggregate) Output	Y	Real GDP
	Output per worker	y = Y/L	Real GDP per capita
	Output per effective worker (E = efficiency)	$\widetilde{y} = Y / EL$	None

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### **Levels vs. Growth Rates**

- Why aggregate (Y) vs. per capita (y = Y/L)?
  - Allows comparisons across countries.
    - Example: Data from 2007

 $Y_{China} = $7,043 \text{ billion} \quad y_{China} = $5,300$ China U.S.  $Y_{US} = $13,860 \text{ billion} \quad y_{US} = $46,000 \text{ Luxemburg} \quad Y_{Lux} = $38.8 \text{ billion} \quad y_{Lux} = $80,800$ 

- Real GDP per capita is the common measure of living standards.
  - Which country above produced the most in 2007?
  - In which does the average worker earn the most?

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### **Levels vs. Growth Rates**

- Why per capita (Y/L) vs. per effective worker (Y/EL)?
  - Useful in the model we will study.
  - Over time, output and output per worker grow.
    - Difficult to define an equilibrium value for a variable that is trending over time.
    - Example: unemployment vs. output per worker.
  - Therefore, while we don't rely on the per effective worker measure for <u>data</u> comparisons, we do use it for developing a theoretical model.
  - Equilibrium value of x is denoted x\* in the model.

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### **Levels vs. Growth Rates**

- How do we study variables that are trending over time? Study the behavior of a variable's growth rate.
- The model we will study uses the following notation to denote the change in a variable, x:

$$\dot{x} = \Delta x$$

Therefore, the growth rate (rate of change) in x is:

$$\dot{x}/x = \Delta x/x$$

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### **Levels vs. Growth Rates**

Note the following rules for dealing with growth rates (we studied these in Chapter 2):

Growth rate of  $(xy) = \frac{\dot{x}}{x} + \frac{\dot{y}}{y}$ 

Growth rate of  $(x/y) = \frac{\dot{x}}{x} - \frac{\dot{y}}{y}$ 

Now, apply this to output per worker, Y/L:

Growth rate of  $(Y/L) = \dot{y}/y = \frac{\dot{Y}}{Y} - \frac{\dot{L}}{L}$ 

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### **Levels vs. Growth Rates**

And for output per effective worker (Y/EL):

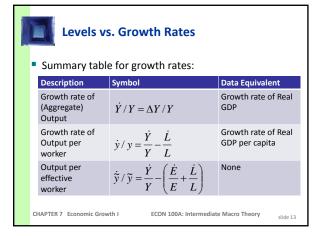
Growth rate of 
$$(Y/EL) = \dot{\tilde{y}}/\tilde{y} = \frac{\dot{Y}}{Y} - (\frac{\dot{E}}{E} + \frac{\dot{L}}{L})$$

- It is important to keep track of notation because we:
  - evaluate how well the theory/model matches data,
  - need to define the equilibrium in the model, and
  - use the model to conduct analyses of different outcomes.

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### The Solow model

- due to Robert Solow, won Nobel Prize for contributions to the study of economic growth
- a major paradigm:
  - widely used in policy making
  - benchmark against which most recent growth theories are compared
- looks at the determinants of economic growth and the standard of living in the long run

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# How Solow model is different from Chapter 3's model

- K is no longer fixed: investment causes it to grow, depreciation causes it to shrink
- L is no longer fixed: population growth causes it to grow
- 3. the consumption function is simpler

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# How Solow model is different from Chapter 3's model

- no G or T
   (only to simplify presentation;
   we can still do fiscal policy experiments)
- 5. notational differences
- 6. E = 1

(per worker and per effective worker are the same; we abstract from how technology affects worker productivity)

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#### The production function

- In aggregate terms: Y = F (K, L)
- Define: y = Y/L = output per workerk = K/L = capital per worker
- Assume constant returns to scale:

zY = F(zK, zL) for any z > 0

■ Pick **z** = **1/L**. Then

Y/L = F(K/L, 1)

y = F(k, 1)

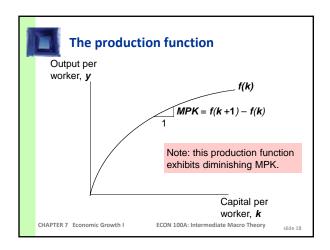
y = f(k)

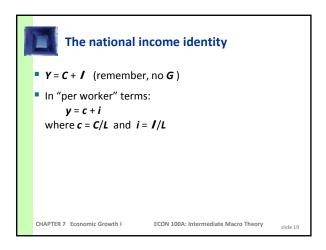
where f(k) = F(k, 1)

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The consumption function

s = the saving rate,
the fraction of income that is saved
(s is an exogenous parameter)

Note: s is the only lowercase variable
that is not equal to
its uppercase version divided by L

Consumption function: c = (1-s)y
(per worker)

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Output, consumption, and investment

Output per worker, y

f(k)

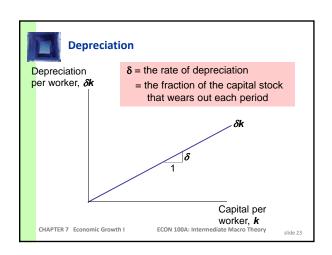
c<sub>1</sub>

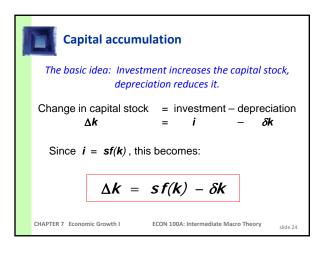
sf(k)

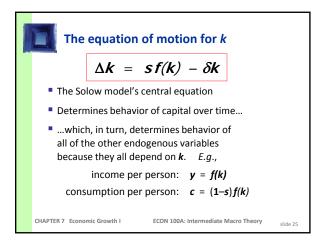
k<sub>1</sub>

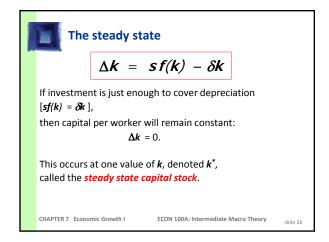
Capital per worker, k

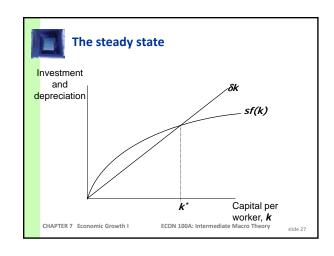
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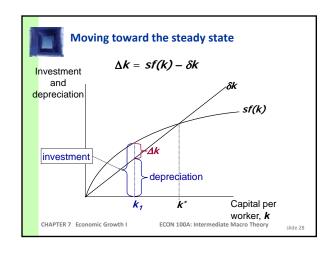


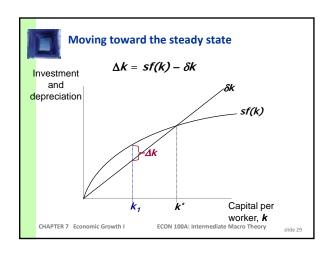


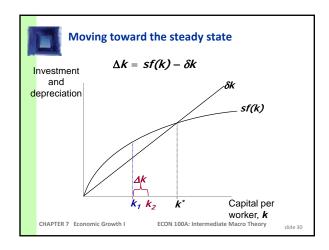


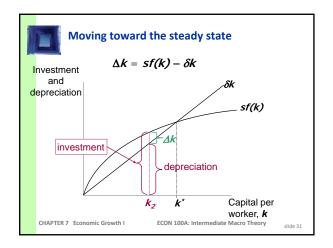


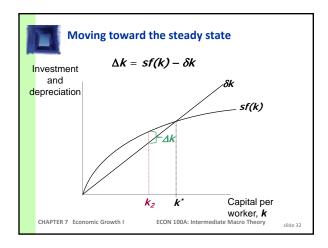


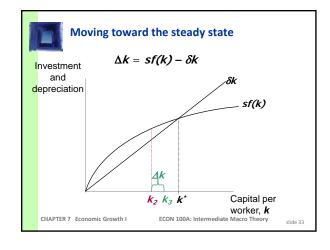


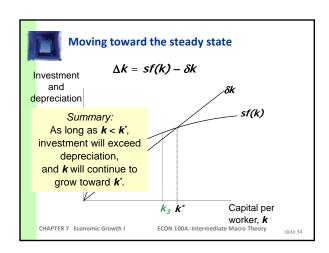


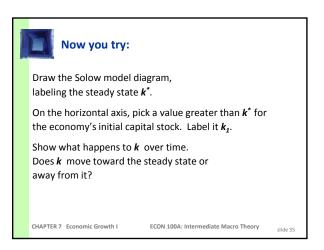














### A numerical example

Production function (aggregate):

$$Y = F(K, L) = \sqrt{K \times L} = K^{1/2}L^{1/2}$$

To derive the per-worker production function, divide through by  $\boldsymbol{L}$ :

$$\frac{\mathbf{Y}}{\mathbf{L}} = \frac{\mathbf{K}^{1/2} \mathbf{L}^{1/2}}{\mathbf{L}} = \left(\frac{\mathbf{K}}{\mathbf{L}}\right)^{1/2}$$

Then substitute y = Y/L and k = K/L to get

$$y = f(k) = k^{1/2}$$

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### A numerical example, cont.

Assume:

- **s** = 0.3
- $\delta = 0.1$
- initial value of k = 4.0

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## Approaching the steady state: A numerical example

 $y = \sqrt{k}$ ; s = 0.3;  $\delta = 0.1$ ; initial k = 4.0Assumptions: i Year k y δk 1 4.000 2.000 1.400 0.600 0.400 0.200 2 4.200 2.049 1.435 0.615 0.420 0.195 3 4.395 2.096 1.467 0.629 0.440 0.189 4.584 2.141 1.499 0.642 0.458 0.184 10 5.602 2.367 1.657 0.710 0.560 0.150 25 7.351 2.706 1.894 0.812 0.732 0.080 100 8.962 2.994 2.096 0.898 0.896 0.002



### **Exercise: Solve for the steady state**

Continue to assume

s = 0.3,  $\delta = 0.1$ , and  $y = k^{1/2}$ 

Use the equation of motion

$$\Delta k = s f(k) - \delta k$$

to solve for the steady-state values of **k**, **y**, and **c**.

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### Solution to exercise:

 $\Delta k = 0$  def. of steady state

3.000 2.100

0.900

0.900

0.000

 $sf(k^*) = \delta k^*$  eq'n of motion with  $\Delta k = 0$ 

 $0.3\sqrt{k^*} = 0.1k^*$  using assumed values

 $3 = \frac{k^*}{\sqrt{k^*}} = \sqrt{k^*}$ 

9.000

Solve to get:  $\mathbf{k}^* = 9$  and  $\mathbf{y}^* = \sqrt{\mathbf{k}^*} = 3$ 

Finally,  $c^* = (1 - s)y^* = 0.7 \times 3 = 2.1$ 

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An increase in the saving rate

An increase in the saving rate raises investment...
...causing k to grow toward a new steady state:

Investment and depreciation

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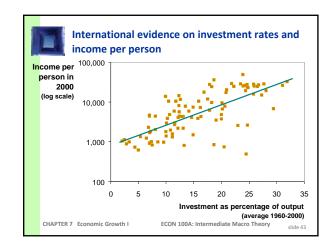
### **Prediction:**

- Higher  $s \Rightarrow$  higher  $k^*$ .
- And since y = f(k), higher  $k^* \Rightarrow$  higher  $y^*$ .
- Thus, the Solow model predicts that countries with higher rates of saving and investment will have higher levels of capital and income per worker in the long run.

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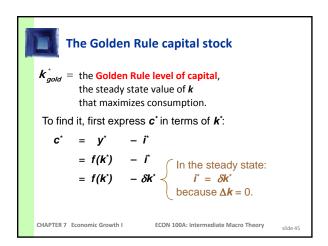
### The Golden Rule: Introduction

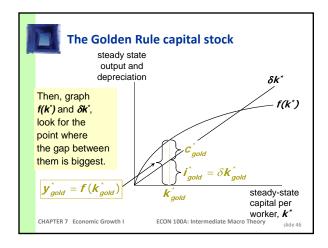
- Different values of s lead to different steady states. How do we know which is the "best" steady state?
- The "best" steady state has the highest possible consumption per person: c\* = (1-s) f(k\*).
- An increase in s
  - leads to higher k\* and y\*, which raises c\*
  - reduces consumption's share of income (1-s), which lowers c\*.
- So, how do we find the s and k\* that maximize c\*?

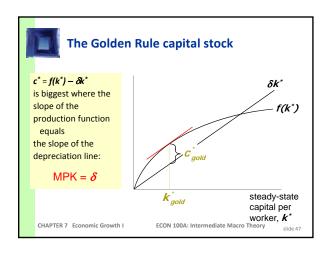
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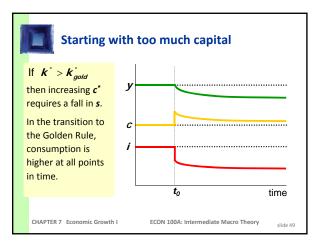
# The transition to the Golden Rule steady state

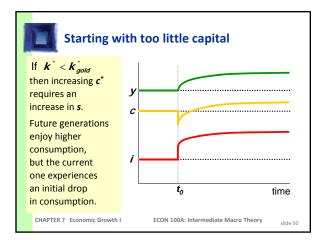
- The economy does NOT have a tendency to move toward the Golden Rule steady state.
- Achieving the Golden Rule requires that policymakers adjust s.
- This adjustment leads to a new steady state with higher consumption.
- But what happens to consumption during the transition to the Golden Rule?

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## **Population growth**

 Assume that the population (and labor force) grow at rate n. (n is exogenous.)

$$\frac{\Delta L}{L} = n$$

- EX: Suppose L = 1,000 in year 1 and the population is growing at 2% per year (n = 0.02).
- Then  $\Delta L = nL = 0.02 \times 1,000 = 20$ , so L = 1,020 in year 2.

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### **Break-even investment**

- (δ+n)k = break-even investment, the amount of investment necessary to keep k constant.
- Break-even investment includes:
  - $\delta k$  to replace capital as it wears out
  - nk to equip new workers with capital (Otherwise, k would fall as the existing capital stock would be spread more thinly over a larger population of workers.)

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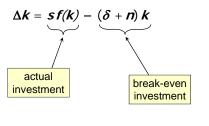
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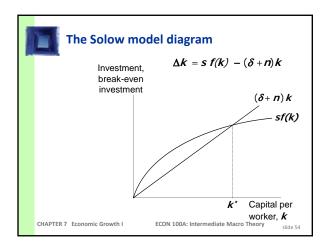
### The equation of motion for k

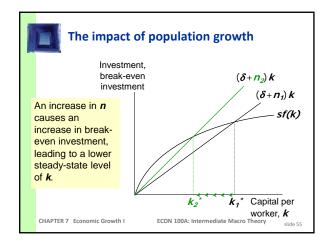
With population growth, the equation of motion for k is

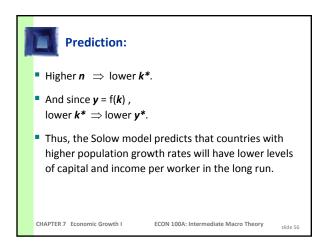


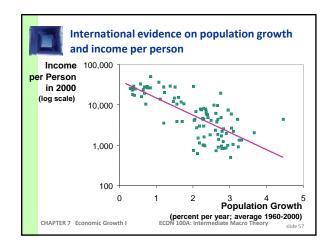
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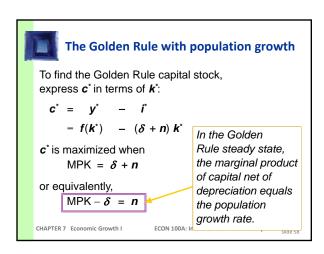
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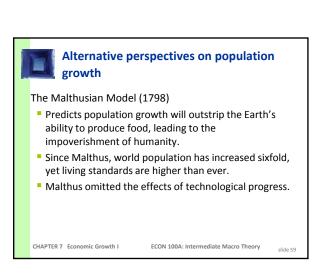














# Alternative perspectives on population growth

The Kremerian Model (1993)

- Posits that population growth contributes to economic growth.
- More people = more geniuses, scientists & engineers, so faster technological progress.
- Evidence, from very long historical periods:
  - As world pop. growth rate increased, so did rate of growth in living standards
  - Historically, regions with larger populations have enjoyed faster growth.

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## **Summary of Part 1 (Lecture 5)**

- 1. The Solow growth model shows that, in the long run, a country's standard of living depends
  - positively on its saving rate
  - negatively on its population growth rate
- 2. An increase in the saving rate leads to
  - higher output in the long run
  - faster growth temporarily
  - but not faster steady state growth.

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## **Summary of Part 1 (Lecture 5)**

3. If the economy has more capital than the Golden Rule level, then reducing saving will increase consumption at all points in time, making all generations better off.

If the economy has less capital than the Golden Rule level, then increasing saving will increase consumption for future generations, but reduce consumption for the present generation.

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